

Factor Theorem: Remember that if $f(a) = 0$, then $(x - a)$ is a factor.

In #1-2, write a polynomial with the given zeros.

1. 4, -9

$$(x-4)(x+9)$$

$$x^2 + 9x - 4x - 36$$

$$\boxed{x^2 + 5x - 36}$$

2. 3, -4, 5

$$(x-3)(x+4)(x-5)$$

$$(x-3)(x^2 - 5x + 4x - 20)$$

$$(x-3)(x^2 - x - 20)$$

$$x^3 - x^2 - 20x$$

$$+ \quad -3x^2 + 3x + 60$$

$$\boxed{x^3 - 4x^2 - 17x + 60}$$

3. 2, -2, 1, 6

$$(x-2)(x+2)(x-1)(x-6)$$

$$(x^2 - 4)(x^2 - 7x + 6)$$

$$x^4 - 7x^3 + 6x^2$$

$$+ \quad -4x^2 + 28x - 24$$

+

$$\boxed{x^4 - 7x^3 + 2x^2 + 28x - 24}$$

- Irrational roots (zeros) and imaginary roots come in conjugate pairs.
- Conjugates are the same expression, just with a different sign (+ or -) in between.
- When using the quadratic formula, you get answers like $(3 \pm \sqrt{2})$ or $(5 \pm 3i)$.
- When solving with square roots, you get answers like $\pm\sqrt{7}$ or $\pm 5i$.
- These are considered conjugate pairs.

In #3-4, suppose that a polynomial has the roots (zeros) listed below. Find two additional roots for the polynomial.

3. $8 + \sqrt{3}$ and $-2i$

$$8 - \sqrt{3}, -2i$$

4. $3 - 5i$ and $\sqrt{7}$

$$3 + 5i, -\sqrt{7}$$

In #5-7, find a polynomial equation that has the given roots.

$$\sqrt{6} \cdot \sqrt{6} = \sqrt{36} = 6$$

5. -5 and $3i$

$$-5, 3i, -3i$$

$$(x+5)(x-3i)(x+3i)$$

$$(x+5)(x^2 - 9i^2)$$

since $i^2 = -1$

$$(x+5)(x^2+9)$$

$$x^3 + 9x + 5x^2 + 45$$

$$\boxed{x^3 + 5x^2 + 9x + 45}$$

6. 2 and $-\sqrt{6}$

$$2, -\sqrt{6}, +\sqrt{6}$$

$$(x-2)(x+\sqrt{6})(x-\sqrt{6})$$

$$(x-2)(x^2-6)$$

$$x^3 - 6x - 2x^2 + 12$$

$$\boxed{x^3 - 2x^2 - 6x + 12}$$

7. $3+2i$, also $3-2i$

$$(x-(3+2i))(x-(3-2i))$$

$$(x-3-2i)(x-3+2i)$$

Distribute 3 times

$$x \rightarrow x^2 - 3x + 2xi$$

$$-3 \rightarrow -3x + 9 - 6i$$

$$-2i \rightarrow -2xi + 6i - 4i^2$$

$$x^2 - 6x + 9 - 4i^2 \quad (xi's \text{ cancel, } i's \text{ cancel})$$

$$i^2 = -1$$

~~$$x^2 - 6x + 9 + 4$$~~

$$x^2 - 6x + 9 + 4$$

$$\boxed{x^2 - 6x + 13}$$