

S.4 Synthetic Division

only works when $\div (x \pm \#)$

$$\textcircled{1} \left(\underline{2x^3} + 13x^2 + 16x + 5 \right) \div \left(\underline{x} + 5 \right)$$

-5	2	13	16	5	-5(2)
↓		-10	-15	-5	-5(3)
	2	3	1	0	

0 → remainder

$$\textcircled{2x^2 + 3x + 1}$$

②

$$\frac{X^4 - 3x^2 + 7x - 1}{X - 2}$$

2		1	0	-3	7	-1
		↓	2	4	2	18
-----		1	2	1	9	17

$X^3 + 2x^2 + 1x + 9$

↓
Remainder

③ Is $(x+a)$ a factor of $f(x)$?

Factor Theorem

$x+a$ is a factor
if $f(-a) = 0$

5.4 Synthetic Division

Only works if $\div (x \pm \#)$

① $(x^3 - 8x^2 + 17x - 10) \div (x - 5)$

$$\begin{array}{r|rrrr} 5 & 1 & -8 & 17 & -10 \\ & & 5 & -15 & 10 \\ \hline & 1 & -3 & 2 & 0 \end{array}$$

S: 1
5(-3)

0 \leftarrow remainder

$$\boxed{x^2 - 3x + 2}$$

$$\textcircled{2} \quad \frac{2x^3 - 4x + 5}{x + 3}$$

$$\begin{array}{r|rrrr} -3 & 2 & 0 & -4 & 5 \\ & \downarrow & -6 & 18 & -42 \\ \hline & 2 & -6 & 14 & \textcircled{-37} \end{array} \rightarrow \text{Remainder}$$

$$2x^2 - 6x + 14 \quad R - 37$$

$$\textcircled{3} \quad (x^4 + 3x - 2) \div (x^1 - 4)$$

4	1	0	0	3	-2	
	↓	4	16	64	268	
		4	16	67	266	
						↓
						R

$1x^3 + 4x^2 + 16x + 67$

④

Factor Theorem

a is an x -intercept

$$f(a) = 0$$

$$(x - a)$$

Is

$(x + 3)$
a factor
of $f(x)$?

check

$$f(-3) = 0$$